



# Intelligent Search Techniques

3<sup>rd</sup> class / العملي

Net, IS, CS Branches

أ.م. سُرى محمود عبدالله

Email: - [Sura.M.abdullah@uotechnology.edu.iq](mailto:Sura.M.abdullah@uotechnology.edu.iq)

Google Site: Google scholar: <https://scholar.google.com/citations?user=ep015F0AAAAJ&hl=en>

Research gate: [https://www.researchgate.net/profile/Sura\\_Abdullah](https://www.researchgate.net/profile/Sura_Abdullah)

# Example6: write a prolog program to append two lists in one list.

## Domains

L= integer\*

## Predicates

app(L,L,L)

## Clauses

app([],L2,L2).

app([H|T1],L2,[H|T3]):-app(T1,L2,T3).

H	
3,	app([4,5],[6,7,5],[3]).
4,	app([5],[6,7,5],[3,4]).
5,	app([], [6,7,5],[3,4,5]).
	app([3,4,5],[6,7,5],[3,4,5,6,7,5]).

## Goal

app([3,4,5],[6,7,5],L).

**Output:** L=[3,4,5,6,7,5]. 1 solution

# Membership Function in List

- Member is possibly the most used user-defined predicate (i.e. you have to define it every time you want to use it).
  - It checks to see if an element is in the list or not.
- it returns **yes** if it is.
- and returns **no** if it isn't.

## Membership formula:

```
member(X,[X|_]).
```

```
member(X,[_|T]) :- member(X,T).
```

- It 1st checks if the first argument unifies with the Head of the list.

If yes then succeed.

If no then fail the first clause.

- The 2nd clause ignores the head of the list (which we know doesn't match) and recurses on the Tail.

*write a prolog program to determine if a specific element in the list or not.*

**domains**

i=integer

l=i\*

**predicates**

member(i,l).

**clauses**

member(X,[X|\_]):-!.

member(X,[\_|T]):- member(X,T).

X

4=1 no, else member(4,[2,4,6,8]).

4=2 no, else member(4,[4,6,8]).

4=4 yes.

**goal**

member(4,[1,2,4,6,8]).

**Output:** yes

**goal:**

member(4,[1,2,6]).

**Output:** no

X

4=1 no, else member(4,[2,6]).

4=2 no, else member(4,[6]).

4=6 no, else member(4,[]).

write prolog program to find the difference between two list such as `diff([1,2,3],[3,4,5],L)`, `L=[1,2]`.

**domains**

`i=integer`

`l=i*`

**predicates**

`diff(l,l,l).`

`member(i,l).`

**clauses**

`diff([],_,[]):-!.`

`diff([H|T],Y,[H|T1]):-not(member(H,Y)),diff(T,Y,T1),!.`

`diff([_|T],Y,Z):-diff(T,Y,Z).`

`member(X,[X|_]):-!.`

`member(X,[_|T]):-member(X,T).`

**goal:** `diff([1,2,3],[3,4,5],L).`

**output:** `L=[1,2]`

# Breadth-First Search Algorithm

## Domains

$c = \text{char.}$

$l = c^*.$

## Predicates

$\text{breadth}(l, l, c).$

$\text{difference}(l, l, l).$

$\text{append}(l, l, l).$

$\text{member}(c, l).$

$\text{print}(l, l).$

$\text{path}(c, c).$

## Clauses

$\text{path}('a', 'b').$

$\text{path}('a', 'c').$

$\text{path}('a', 'd').$

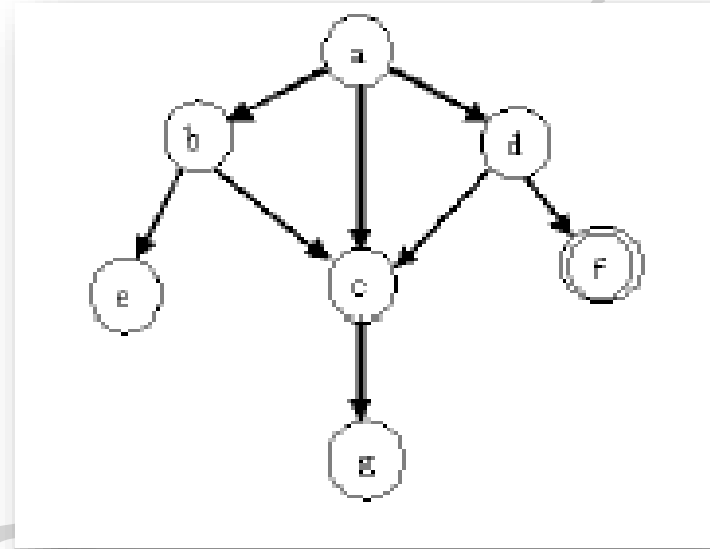
$\text{path}('b', 'e').$

$\text{path}('b', 'c').$

$\text{path}('d', 'c').$

$\text{path}('d', 'f').$

$\text{path}('c', 'g').$





```
breadth([],_,_):-!,write("Goal is not found ").
```

```
breadth([G|T_Open],Closed,G):-!,print([G|T_Open],Closed),write("Goal is  
found "),nl.
```

```
breadth([H|T_Open],Closed,G):-print([H|T_Open],Closed),  
    findall(X,path(H,X),Children),  
    append(Closed,[H],Closed1),  
    difference(Children,T_Open,Children1),  
    difference(Children1,Closed1,Children2),  
    append(T_Open,Children2,Open1),  
    breadth(Open1,Closed1,G).
```

```
difference([],_,[]):- !.
```

```
difference([H|T],Z,[H|T1]):- not(member(H,Z)),!, difference(T,Z,T1).
```

```
difference([_|T],Z,T1):- difference(T,Z,T1).
```

```
member(H,[H|_]):-!.
```

```
member(H,[_|T]):- member(H,T).
```

```
append([],L,L):-!.
```

```
append([H|T],L,[H|M]):- append(T,L,M).
```

```
print(Open,Closed):- write("Open=",Open," ","Closed=",Closed),nl.
```

Goal: breadth(['a'],[],'f').

- Open=['a']                      Closed=[]
- Open=['b','c','d']            Closed=['a']
- Open=['c','d','e']            Closed=['a','b']
- Open=['d','e','g']            Closed=['a','b','c']
- Open=['e','g','f']            Closed=['a','b','c','d']
- Open=['g','f']                Closed=['a','b','c','d','e']
- Open=['f']                    Closed=['a','b','c','d','e','g']
  
- Goal is found

# Depth-First Search Algorithm

## Domains

$c = \text{char.}$

$l = c^*$ .

## Predicates

$\text{depth}(l, l, c).$

$\text{difference}(l, l, l).$

$\text{append}(l, l, l).$

$\text{member}(c, l).$

$\text{print}(l, l).$

$\text{path}(c, c).$

## Clauses

$\text{path}('a', 'b').$

$\text{path}('a', 'c').$

$\text{path}('a', 'd').$

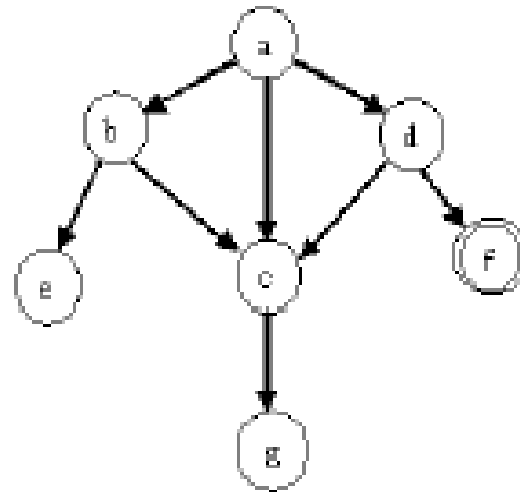
$\text{path}('b', 'e').$

$\text{path}('b', 'c').$

$\text{path}('d', 'c').$

$\text{path}('d', 'f').$

$\text{path}('c', 'g').$



```
depth([],_,_):-!,write("Goal is not found ").
```

```
depth([G|T_Open],Closed,G):-!,print([G|T_Open],Closed),write("Goal is  
found "),nl.
```

```
depth([H|T_Open],Closed,G):- print([H|T_Open],Closed),  
    findall(X,path(H,X),Children),  
    append(Closed,[H],Closed1),  
    difference(Children,T_Open,Children1),  
    difference(Children1,Closed1,Children2),  
    append(Children2,T_Open,Open1),  
    depth(Open1,Closed1,G).
```

```
difference([],_,[]):- !.
```

```
difference([H|T],Z,[H|T1]):- not(member(H,Z)),!, difference(T,Z,T1).
```

```
difference(_|T,Z,T1):- difference(T,Z,T1).
```

```
member(H,[H|_]):-!.
```

```
member(H,[_|T]):- member(H,T).
```

```
append([],L,L):-!.
```

```
append([H|T],L,[H|M]):- append(T,L,M).
```

```
print(Open, Closed):- write("Open=",Open," ","Closed=",Closed),nl.
```

Goal: depth(['a'],[],'f').

- Open=['a']                      Closed=[]
- Open=['b','c','d']            Closed=['a']
- Open=['e','c','d']            Closed=['a','b']
- Open=['c','d']                Closed=['a','b','e']
- Open=['g','d']                Closed=['a','b','e','c']
- Open=['d']                    Closed=['a','b','e','c','g']
- Open=['f']                    Closed=['a','b','e','c','g','d']
  
- Goal is found



**Example: write a prolog program to find the minimum number in the list.**

**Domains**

i=integer

l= i\*

**Predicates**

min( l,i,i)

**Clauses**

min([],M,M).

min([H|T],X,M):-H<X,!, min(T,H,M).

min([\_|T],X,M):- min(T,X,M).

H	X		
3	< 15	yes	max([9,4,5],3,M).
9	< 3	no	max([4,5],3,M).
4	< 3	no else	max([5],3,M).
5	< 3	no else	max([],3,M).

**Goal**

min([3,9,4,5],15,M).

**Output:** M=3.

1 solution

**Example: write a prolog program to delete a specific element from list.**

**domains**

i=integer

l=i\*

**predicates**

del(i,l,l).

**clauses**

del(\_,[],[]):-!.

del(X,[H|T],L):- X=H, !,del(X,T,L).

del(X,[H|T],[H|T1]):-del(X,T,T1).

x	H	
3	= 1	no, else del(3,[3,4,3],[1]).
3	= 3	yes, del(3,[4,3],[1]).
3	= 4	no, else del(3,[3],[1,4]).
3	= 3	yes, del(3,[],[1,4]).

**Goal**

del(3,[1,3,4,3],L).

output: L=[1,4].

1 solution

**Example:** *write a prolog program to sort the list elements in ascending order.*

**domains**

i=integer

l=i\*

**predicates**

min(l, i, i)

del(i, l, l)

sort(l, l)

**clauses**

sort([], []).

sort(L, [M | T]):-min(L, 100, M), del(M, L, Z), sort(Z, T), !.

min([], M, M).

min([H | T], X, M):-H < X, min(T, H, M), !.

min([\_ | T], X, M):-min(T, X, M).

del(\_, [], []).

del(X, [H | T], L):-X = H, del(X, T, L).

del(X, [H | T], [H | T1]):-del(X, T, T1), !.

**Goal:** sort ([5,4,9,7,3], L).

**Output:** L=[3,4,5,7,9]

# Hill Climbing Algorithm

## domains

f=s(char,integer).

l=f\*.

c=char.

i=integer.

## predicates

hill(l,l,c).

append(l,l,l).

sort(l,l).

sum(l,i).

min(l,f).

del(f,l,l).

print(l,l).

dead\_end(l,f).

equal\_cost(l).

path(f,f).

## clauses

path(s('a',0),s('b',4)).

path(s('a',0),s('c',5)).

path(s('a',0),s('d',3)).

path(s('b',4),s('e',3)).

path(s('b',4),s('c',1)).

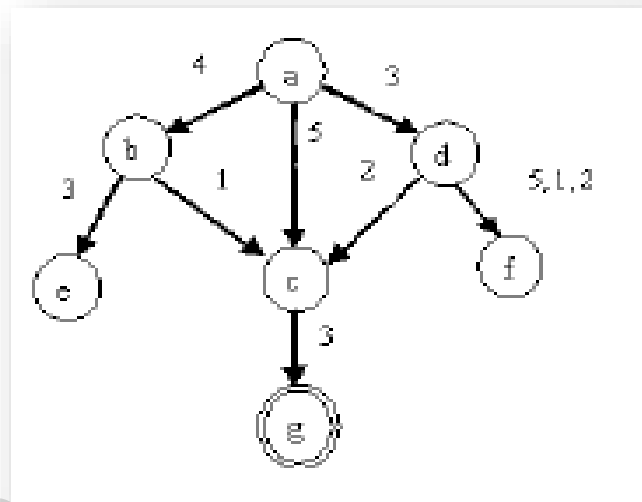
path(s('d',3),s('c',2)).

path(s('d',3),s('f',5)).

path(s('c',1),s('g',3)).

path(s('c',5),s('g',3)).

path(s('c',2),s('g',3)).



```
hill([],_,_):-!,write("The goal is not found").
hill([s(G,H)|T_Open],Closed,G):-!, print([s(G,H)|T_Open],Closed), append(Closed,[s(G,H)],Path),
    write("Goal is found & the resulted path is ",Path), nl,
    sum(Path,N),write("Total cost=",N).
```

```
hill([H|T_Open],Closed,G):- print([H|T_Open],Closed), findall(X,path(H,X),Children),
    not(dead_end(Children,H)), append(Closed,[H],Closed1),
    sort(Children,S_children), not(equal_cost(S_children)),
    append(S_children,T_Open,Open1), hill(Open1,Closed1,G).
```

```
append([],L,L):-!.
append([H|T],L,[H|T1]):- append(T,L,T1).
```

```
sum([],0).
sum([s(_,H)|T],N):- sum(T,N1), N=N1+H.
```

```
sort([],[]):-!.
sort(L,[M|T]):- min(L,M), del(M,L,X), sort(X,T).
```

```
min([M],M):-!.
min([s(A,X),s(_,Y)|T],M):- X<=Y,!, min([s(A,X)|T],M).
min([_|T],M):- min(T,M).
```

```
del(X,[X|T],T):-!.
del(X,[H|T],[H|T1]):- del(X,T,T1).
```

```
dead_end([],H):- write("Serch is stopped because there is dead  
end= ",H), nl.
```

```
equal_cost([s(A,X),s(B,X)|_]):- S1=s(A,X),S2=s(B,X),  
write("Search is stopped because there are equal costs for the  
states= ",S1,"&",S2), nl.
```

```
print(Open,Closed):- write("Open=",Open," ", "Closed=",Closed),nl.
```

```
/* goal: hill([s('a',0)],[],'g').
```

```
Open=[s('a',0)] Closed=[]
```

```
Open=[s('d',3),s('b',4),s('c',5)] Closed=[s('a',0)]
```

```
Open=[s('c',2),s('f',5),s('b',4),s('c',5)] Closed=[s('a',0),s('d',3)]
```

```
Open=[s('g',3),s('f',5),s('b',4),s('c',5)] Closed=[s('a',0),s('d',3),s('c',2)]
```

```
Goal is found & the resulted path is [s('a',0),s('d',3),s('c',2),s('g',3)]
```

```
Total cost=8 */
```

```
/* goal: hill([s('a',0)],[],'g').%path(s('d',3),s('f',1)).
```

```
Open=[s('a',0)] Closed=[]
```

```
Open=[s('d',3),s('b',4),s('c',5)] Closed=[s('a',0)]
```

```
Open=[s('f',1),s('c',2),s('b',4),s('c',5)] Closed=[s('a',0),s('d',3)]
```

```
Search is stopped because there is dead end= s('f',1) */
```

```
/*goal: hill([s('a',0)],[],'g').%path(s('d',3),s('f',2)).
```

```
Open=[s('a',0)] Closed=[]
```

```
Open=[s('d',3),s('b',4),s('c',5)] Closed=[s('a',0)]
```

```
Search is stopped because there are equal costs for the states=  
s('c',2)&s('f',2) */
```



# Best First Search Algorithm

## Domains

$f = s(\text{char}, \text{integer})$ .

$l = f^*$ .

$c = \text{char}$ .

$i = \text{integer}$ .

## Predicates

$\text{best}(l, l, c)$ .

$\text{difference}(l, l, l)$ .

$\text{member}(f, l)$ .

$\text{append}(l, l, l)$ .

$\text{best\_open}(l, l, l)$ .

$\text{set\_best}(f, l, l)$ .

$\text{best\_closed}(l, l, l)$ .

$\text{remove\_worst}(f, l, l)$ .

$\text{best\_children}(l, l, l)$ .

$\text{ignore\_worst}(f, l, l)$ .

$\text{check}(l, l, l, l, l)$ .

$\text{sort}(l, l)$ .

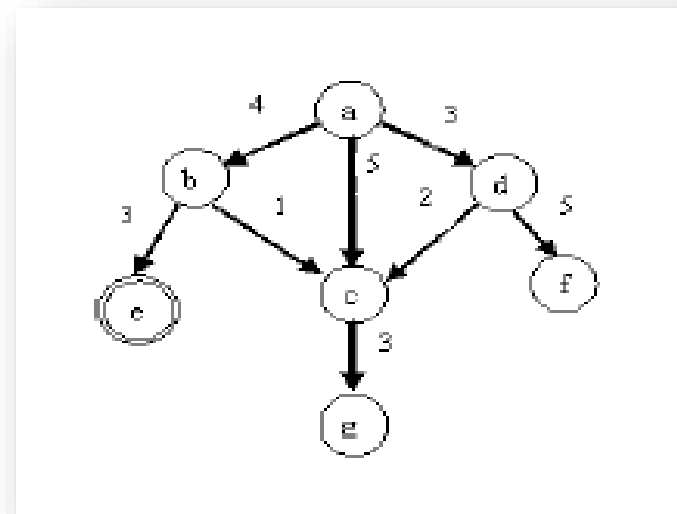
$\text{min}(l, f)$ .

$\text{del}(f, l, l)$ .

$\text{sum}(l, i)$ .

$\text{print}(l, l)$ .

$\text{path}(f, f)$ .



## clauses

```
path(s('a',0),s('b',4)).
path(s('a',0),s('c',5)).
path(s('a',0),s('d',3)).
path(s('b',4),s('e',3)).
path(s('b',4),s('c',1)).
path(s('d',3),s('c',2)).
path(s('d',3),s('f',5)).
path(s('c',1),s('g',3)).
path(s('c',5),s('g',3)).
path(s('c',2),s('g',3)).
best([],_,_):-!,write("The goal is not found").
best([s(G,H)|T],Closed,G):-!, print([s(G,H)|T],Closed),
    append(Closed,[s(G,H)],Path),
    write("The goal is found &The resulted path is ",Path),nl,
    sum(Path,N),write("Total cost=",N),nl.

best([H|T_Open],Closed,G):- print([H|T_Open],Closed), findall(X,path(H,X),Children),
    check(Children,T_Open,Closed,Open1,Closed1),
    sort(Open1,Open2), append(Closed1,[H],Closed2),
    best(Open2,Closed2,G).
```

check(Children,Open,Closed,New\_Open,Closed):-  
difference(Children,Open,X),  
difference(X,Closed,Y),  
Children=Y,!,  
append(Children,Open,New\_Open).

check(Children,Open,Closed,New\_Open,Closed):-  
difference(Children,Open,X),not(Children=X),!,  
best\_open(Children,Open,Open1),  
append(X,Open1,New\_Open).

check(Children,Open,Closed,New\_Open,New\_closed):-  
best\_closed(Children,Closed,New\_closed),  
best\_children(Closed,Children,Best\_child),  
append(Best\_child,Open,New\_Open).

difference([],\_,[]):- !.

difference([H|T],Z,[H|T1]):- not(member(H,Z)),!, difference(T,Z,T1).

difference([\_|T],Z,T1):- difference(T,Z,T1).

member(s(A,\_),[s(A,\_)|\_]):-!.

member(H,[\_|T]):- member(H,T).

append([],L,L):-!.

append([H|T],X,[H|T1]):- append(T,X,T1).

best\_open([],Z,Z):-!.

best\_open([X|T],Y,Z):- set\_best(X,Y,Z1), best\_open(T,Z1,Z).

set\_best(\_,[],[]):-!.

set\_best(s(A,X),[s(A,Y)|T],[s(A,X)|T]):- X<Y,!.

set\_best(X,[H|T],[H|Z]):- set\_best(X,T,Z).

best\_closed([],Z,Z):-!.

best\_closed([X|T],Y,Z):- remove\_worst(X,Y,Z1), best\_closed(T,Z1,Z).

remove\_worst(\_,[],[]):-!.

remove\_worst(s(A,X),[s(A,Y)|T],T):- Y>X,!.

remove\_worst(X,[H|T],[H|Z]):- remove\_worst(X,T,Z).

```
best_children([],Z,Z):-!.
```

```
best_children([X|T],Y,Z):- ignore_worst(X,Y,Z1), best_children(T,Z1,Z).
```

```
ignore_worst(_,[],[]):-!.
```

```
ignore_worst(s(A,X),[s(A,Y)|T],T):- Y>=X,!.
```

```
ignore_worst(X,[H|T],[H|Z]):- ignore_worst(X,T,Z).
```

```
sort([],[]):-!.
```

```
sort(L,[M|T]):- min(L,M), del(M,L,X), sort(X,T).
```

```
min([M],M):-!.
```

```
min([s(A,X),s(_Y)|T],M):- X<=Y,! , min([s(A,X)|T],M).
```

```
min([_|T],M):- min(T,M).
```

```
del(X,[X|T],T):-!.
```

```
del(X,[H|T],[H|T1]):- del(X,T,T1).
```

```
sum([],0).
```

```
sum([s(_H)|T],N):- sum(T,N1),N=N1+H.
```

```
print(Open,Closed):- write("Open=",Open," ","Closed=",Closed),nl.
```

```
/* goal:best([s('a',0)],[],'e').
```

```
Open=[s('a',0)]
```

```
Open=[s('d',3),s('b',4),s('c',5)]
```

```
Open=[s('c',2),s('b',4),s('f',5)]
```

```
Open=[s('g',3),s('b',4),s('f',5)]
```

```
Open=[s('b',4),s('f',5)]
```

```
Open=[s('c',1),s('e',3),s('f',5)]
```

```
Open=[s('e',3),s('f',5)]
```

```
Closed=[]
```

```
Closed=[s('a',0)]
```

```
Closed=[s('a',0),s('d',3)]
```

```
Closed=[s('a',0),s('d',3),s('c',2)]
```

```
Closed=[s('a',0),s('d',3),s('c',2),s('g',3)]
```

```
Closed=[s('a',0),s('d',3),s('g',3),s('b',4)]
```

```
Closed=[s('a',0),s('d',3),s('g',3),s('b',4),s('c',1)]
```

The goal is found &The resulted path is [s('a',0),s('d',3),s('g',3),s('b',4),s('c',1),s('e',3)]

Total cost=14

```
yes */
```

# A Search Algorithm



## domains

$f = s(\text{char}, \text{integer}, \text{integer})$ .

$l = f^*$ .

$c = \text{char}$ .

$i = \text{integer}$ .

## predicates

$a\_algo(l, l, c)$ .

$\text{difference}(l, l, l)$ .

$\text{member}(f, l)$ .

$\text{append}(l, l, l)$ .

$\text{best\_open}(l, l, l)$ .

$\text{set\_best}(f, l, l)$ .

$\text{best\_closed}(l, l, l)$ .

$\text{remove\_worst}(f, l, l)$ .

$\text{best\_children}(l, l, l)$ .

$\text{ignore\_worst}(f, l, l)$ .

$\text{check}(l, l, l, l, l)$ .

$\text{sort}(l, l)$ .

$\text{min}(l, f)$ .

$\text{del}(f, l, l)$ .

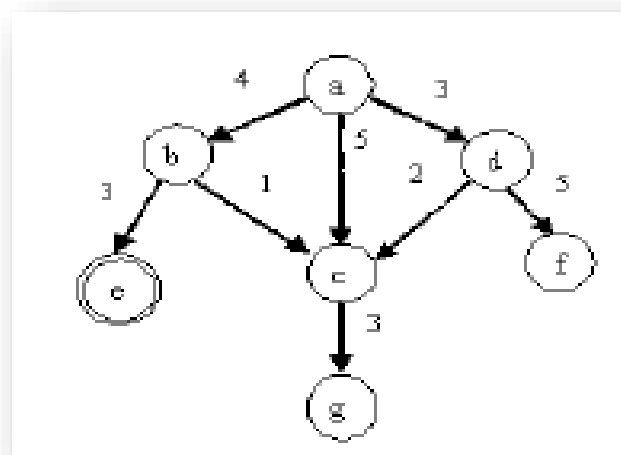
$a\_sum(l, l)$ .

$\text{original\_cost}(l, l)$ .

$\text{sum}(l, i)$ .

$\text{print}(l, l)$ .

$\text{path}(f, f)$ .



## clauses

```
path(s('a',0,0),s('b',4,1)).
```

```
path(s('a',0,0),s('c',5,1)).
```

```
path(s('a',0,0),s('d',3,1)).
```

```
path(s('b',4,1),s('e',3,2)).
```

```
path(s('b',4,1),s('c',1,2)).
```

```
path(s('d',3,1),s('c',2,2)).
```

```
path(s('d',3,1),s('f',5,2)).
```

```
path(s('c',1,2),s('g',3,3)).
```

```
path(s('c',5,1),s('g',3,2)).
```

```
path(s('c',2,2),s('g',3,3)).
```

```
a_algo([],_,_):-!,write("The goal is not found").
```

```
a_algo([s(G,B,C)|T],Closed,G):-!, print([s(G,B,C)|T],Closed),
```

```
    append(Closed,[s(G,B,C)],Path),
```

```
    original_cost(Path,Path1),
```

```
    write("The goal is found &The resulted path=",Path1),nl,
```

```
    sum(Path1,N),write("Total cost=",N),nl.
```

```
a_algo([s(A,B,C)|T_Open],Closed,G):- print([s(A,B,C)|T_Open],Closed),Q=B-C,  
    findall(X,path(s(A,Q,C),X),Children),  
    a_sum(Children,Children1),  
    check(Children1,T_Open,Closed,Open1,Closed1),  
    sort(Open1,Open2),  
    append(Closed1,[s(A,B,C)],Closed2),  
    a_algo(Open2,Closed2,G).
```

```
check(Children,Open,Closed,New_Open,Closed):- difference(Children,Open,X),  
    difference(X,Closed,Y), Children=Y,!,  
    append(Children,Open,New_Open).
```

```
check(Children,Open,Closed,New_Open,Closed):- difference(Children,Open,X),  
    not(Children=X),!,  
    best_open(Children,Open,Open1),  
    append(X,Open1,New_Open).
```

```
check(Children,Open,Closed,New_Open,New_closed):-  
    best_closed(Children,Closed,New_closed),  
    best_children(Closed,Children,Best_children),  
    append(Best_children,Open,New_Open).
```

```
difference([],_,[]):- !.  
difference([H|T],Z,[H|T1]):- not(member(H,Z)),!, difference(T,Z,T1).  
difference([_|T],Z,T1):- difference(T,Z,T1).
```

```
member(s(A,_,_),[s(A,_,_)|_]):-!.  
member(H,[_|T]):- member(H,T).
```

```
append([],L,L):-!.  
append([H|T],X,[H|T1]):- append(T,X,T1).
```

```
best_open([],Z,Z):-!.  
best_open([X|T],Y,Z):- set_best(X,Y,Z1), best_open(T,Z1,Z).
```

```
set_best(_,[],[]):-!.  
set_best(s(A,B1,C),[s(A,B2,_)|T],[s(A,B1,C)|T]):- B1<B2,!.  
set_best(X,[H|T],[H|Z]):- set_best(X,T,Z).
```

```
best_closed([],Z,Z):-!.  
best_closed([X|T],Y,Z):- remove_worst(X,Y,Z1), best_closed(T,Z1,Z).
```

```
remove_worst(_,[],[]):-!.  
remove_worst(s(A,B1,_),[s(A,B2,_)|T],T):- B2>B1,!.  
remove_worst(X,[H|T],[H|Z]):- remove_worst(X,T,Z).
```

```
best_children([],Z,Z):-!.
best_children([X|T],Y,Z):- ignore_worst(X,Y,Z1), best_children(T,Z1,Z).

ignore_worst(_,[],[]):-!.
ignore_worst(s(A,B1,_),[s(A,B2,_)|T],T):- B2>=B1,!.
ignore_worst(X,[H|T],[H|Z]):- ignore_worst(X,T,Z).

sort([],[]):-!.
sort(L,[M|T]):- min(L,M), del(M,L,X), sort(X,T).

min([M],M):-!.
min([s(A,B1,C),s(_B2,_)|T],M):- B1<=B2,!, min([s(A,B1,C)|T],M).
min(_|T,M):- min(T,M).

del(X,[X|T],T):-!.
del(X,[H|T],[H|T1]):- del(X,T,T1).

a_sum([],[]):-!.
a_sum([s(A,B1,C)|T],[s(A,B2,C)|T1]):- B2=B1+C, a_sum(T,T1).

original_cost([],[]):-!.
original_cost([s(A,B1,C)|T],[s(A,B2,C)|T1]):-B2=B1-C, original_cost(T,T1).

sum([],0).
sum([s(_B,_)|T],N):- sum(T,N1),N=N1+B.

print(Open,Closed):- write("Open=",Open," ","Closed=",Closed),nl.
```

```
/* goal: a_algo([s('a',0,0)],[],'e').
```

```
Open=[s('a',0,0)]
```

```
Open=[s('d',4,1),s('b',5,1),s('c',6,1)]
```

```
Open=[s('c',4,2),s('b',5,1),s('f',7,2)]
```

```
Open=[s('b',5,1),s('g',6,3),s('f',7,2)]
```

```
Open=[s('c',3,2),s('e',5,2),s('g',6,3),s('f',7,2)]
```

```
Open=[s('e',5,2),s('g',6,3),s('f',7,2)]
```

```
Closed=[]
```

```
Closed=[s('a',0,0)]
```

```
Closed=[s('a',0,0),s('d',4,1)]
```

```
Closed=[s('a',0,0),s('d',4,1),s('c',4,2)]
```

```
Closed=[s('a',0,0),s('d',4,1),s('b',5,1)]
```

```
Closed=[s('a',0,0),s('d',4,1),s('b',5,1),s('c',3,2)]
```

```
The goal is found &The resulted path=[s('a',0,0),s('d',3,1),s('b',4,1),s('c',1,2),s('e',3,2)]
```

```
Total cost=11
```

```
Yes */
```